



8. kongres Hrvatskog društva za medicinsku biokemiju i  
laboratorijsku medicinu s međunarodnim sudjelovanjem  
22. – 26. rujna 2015., Rijeka, Hrvatska

# Statistička usporedba mjernih postupaka

Mladen Petrovečki

Klinički zavod za laboratorijsku dijagnostiku Kliničke bolnice Dubrava,  
Zagreb; Katedra za medicinsku informatiku, Medicinski fakultet  
Sveučilišta u Rijeci





# Uvod



# Usporedba mjerenja

- brojnost, količina, sadržaj, koncentracija
  - iste tvari u kliničkom laboratoriju ili
  - (općenito) istog pokazatelja (variable) u znanstvenom istraživanju
- usporedba posebnim statističkim postupcima
  - uspoređuju **isti** pokazatelj u dva (ili više) mjerjenja
  - ista skupina ispitanika,
  - različiti mjerni sustavi  
(uredaj, instrument, test, upitnik...)



# Koeficijenti korelacija brojčanih pokazatelja

- Pearsonov koeficijent korelacijske (r,  $r_p$ )
- Spearmanov koeficijent korelacijske rangova (r,  $r_s$ )
- Kendallov koeficijent korelacijske rangova (Kendallov  $\tau$ )
- biserijski koeficijent ( $r_{PB}$ )
- koeficijent eta ( $\eta$ )
- koeficijent višestruke korelacijske (R)



# Koeficijenti korelacija kategoričkih pokazatelja

- koeficijent  $\phi$
- Pearsonov koeficijent kontingencije C
- Cramerov V
- Tschuprowljev T
- koeficijent  $\lambda$  Goodmana i Kruskala



# Mjere podudarnosti

- kategorički pokazatelji
  - ❑ Linov koeficijent konkordancije W
  - ❑ interklasni koeficijent korelacije (ICC, engl. *interclass correlation coefficient*)
  - ❑ koeficijent ponovljivosti (BSI, engl. *British Standards Institute repeatability coefficient*)
  - ❑ Cohenov kappa ( $\kappa$ )
- grafički postupci
  - ❑ Bland-Altmanov grafikon
  - ❑ grafikon Krouwera i Montijeve



# Regresijski postupci

- jednostavna regresija  
(linearna, polinomska, semilogaritamska...)
- višestruka linearna regresija
- logistička regresija
- Coxova regresija proporcionalnih rizika
- Passing-Bablokova regresija
- Demingova regresija



# Regresijski postupci

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- Passing-Bablokova regresija
  - Demingova regresija



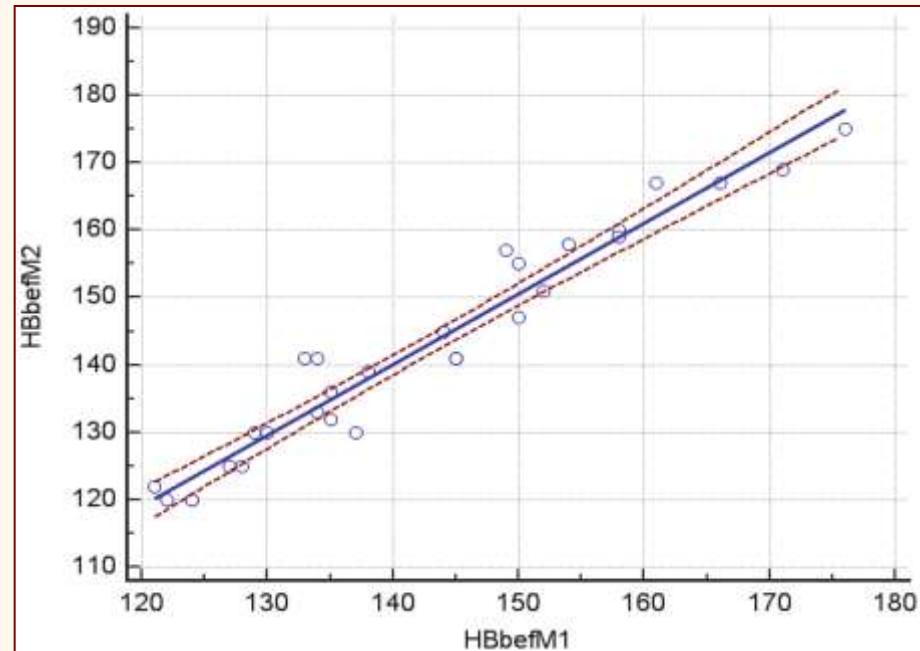


# Nekoliko primjera

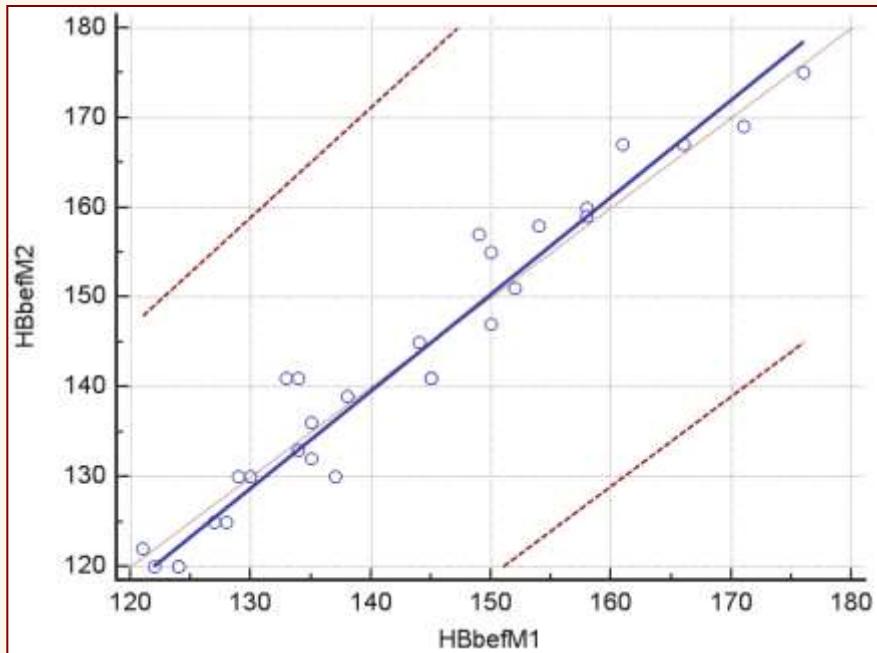


# Korelacija i linearna regresija

- hemoglobin (g/L)
- N = 29
- $r = 0,973$  ( $0,943 - 0,987$ ; 95%CI)
- $P < 0,001$
- $y = -6,99 \pm 6,87 + 1,05 \pm 0,05 x$



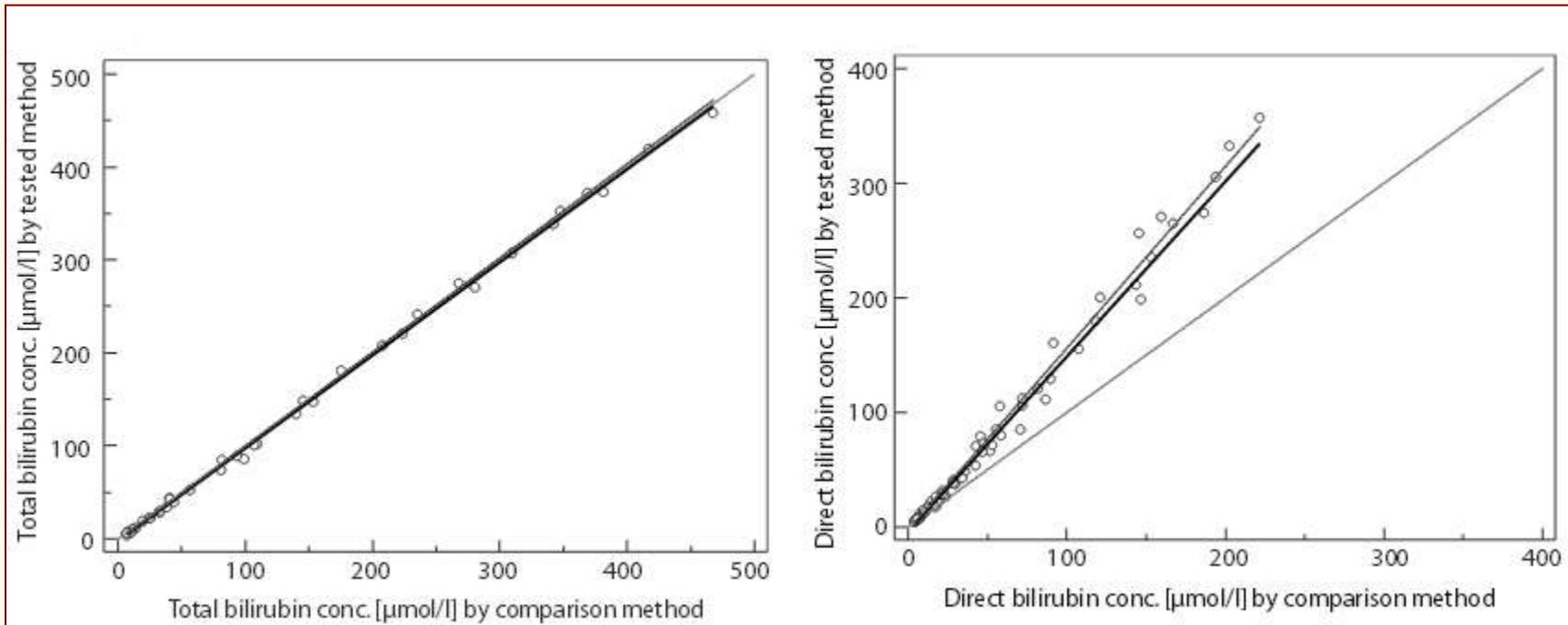
# Passing-Bablokova regresija



Variable X	HBbefM1	
Variable Y	HBbefM2	
Sample size	29	
<b>Regression Equation</b>		
$y = -12,166667 + 1,083333 \times$		
<b>Systematic differences</b>		
Intercept A	-12,1667	
95% CI	-31,0000 to 0,0000	
<b>Proportional differences</b>		
Slope B	1,0833	
95% CI	1,0000 to 1,2222	
<b>Random differences</b>		
Residual Standard Deviation (RSD)	2,6643	
$\pm 1.96$ RSD Interval	-5,2220 to 5,2220	
<b>Linear model validity</b>		
Cusum test for linearity	No significant deviation from linearity (P=0,86)	



# Passing-Bablokova regresija



N  
raspon mjerena ( $\mu\text{mol/L}$ )  
 $r$   
jednadžba (95%CI)  
"cusum" test

40  
3 – 468  
0,99 ( $P < 0,001$ )  
 $y = -3.0 \text{ (-3.8 - -2.1)} + 1.00 \text{ (0.98 - 1.01)} x$   
 $P > 0.1$

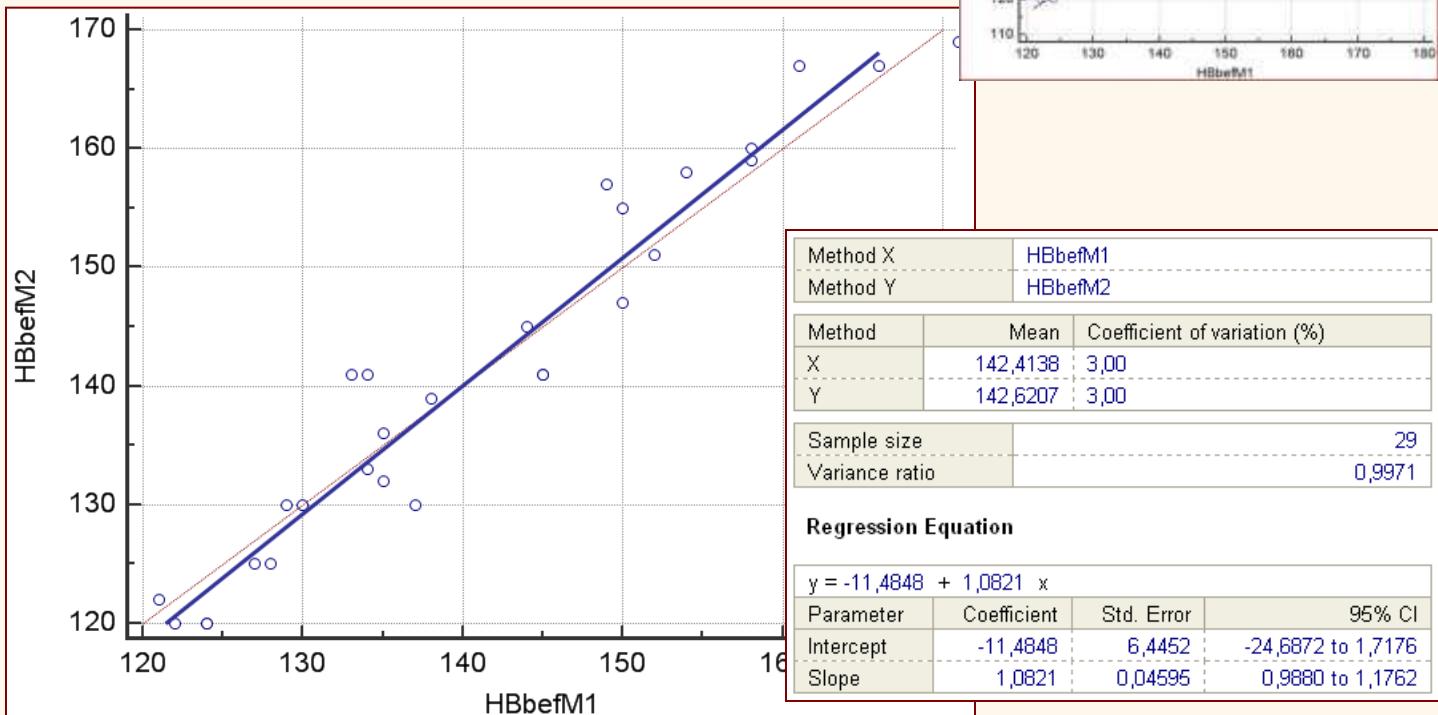
N  
raspon mjerena ( $\mu\text{mol/L}$ )  
 $r$   
jednadžba (95%CI)  
"cusum" test

70  
4 – 357  
0,99 ( $P < 0,001$ )  
 $y = -3.2 \text{ (-4.2 - -1.9)} + 1.52 \text{ (1.47 - 1.58)} x$   
 $P < 0,01$

Bilić-Zulle L. Comparison of methods: Passing and Bablok regression. Biochimia Medica 2011;21(1):49–52.



# Demingova regresija



- parametrijska analiza
- normalna raspodjela podataka



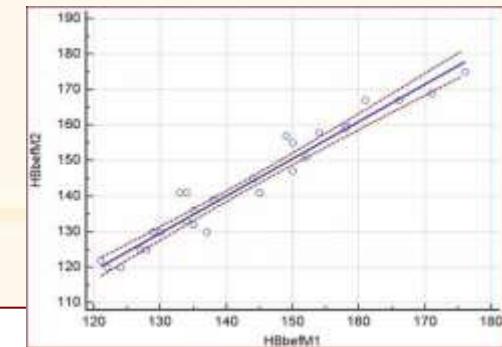
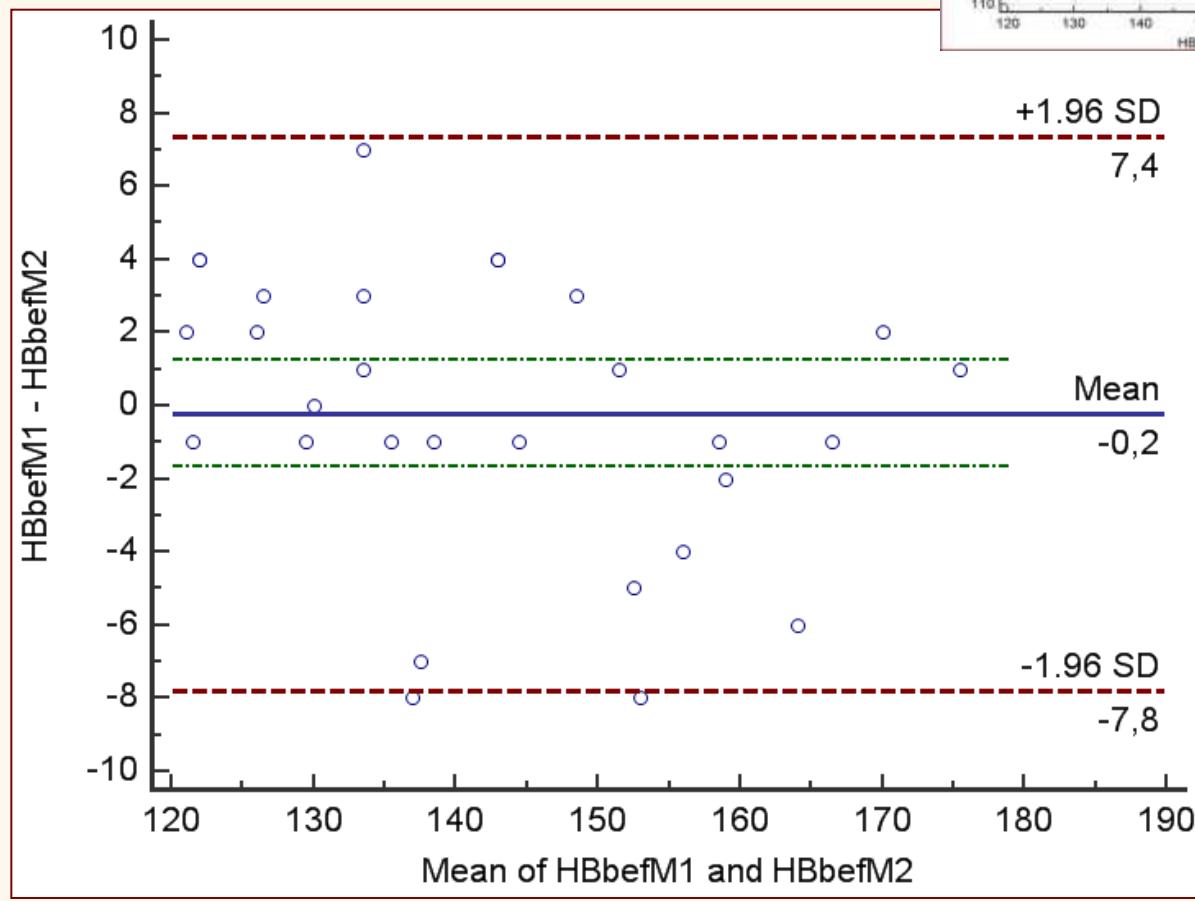
# Demingova regresija

Method X	HBbefM1				
Method Y	HBbefM2				
Method	Mean	Coefficient of variation (%)			
X	142,4138	6,00			
Y	142,6207	3,00			
Sample size			29		
Variance ratio			3,9884		
<b>Regression Equation</b>					
$y = -13,9373 + 1,0993 \times$					
Parameter	Coefficient	Std. Error	95% CI		
Intercept	-13,9373	6,7274	-27,7177 to -0,1569		
Slope	1,0993	0,04836	1,0003 to 1,1984		

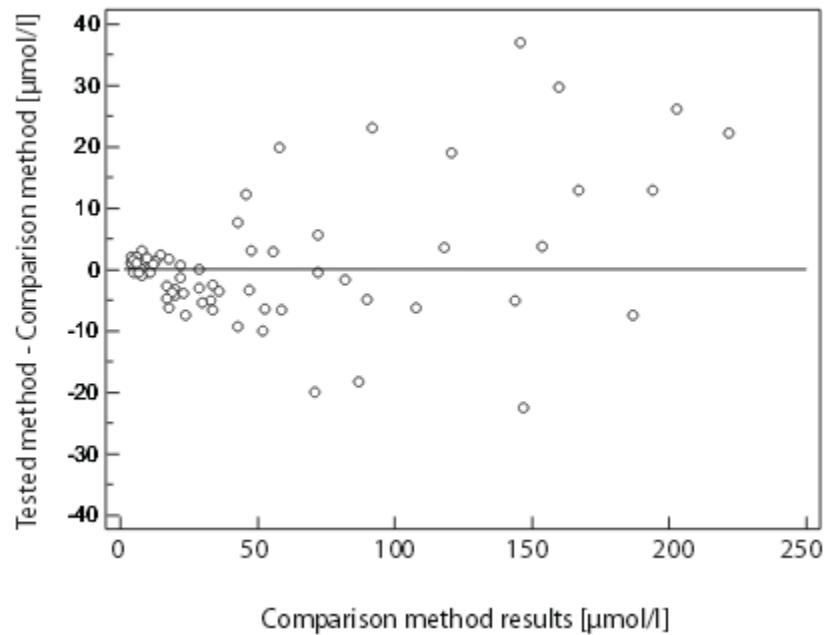
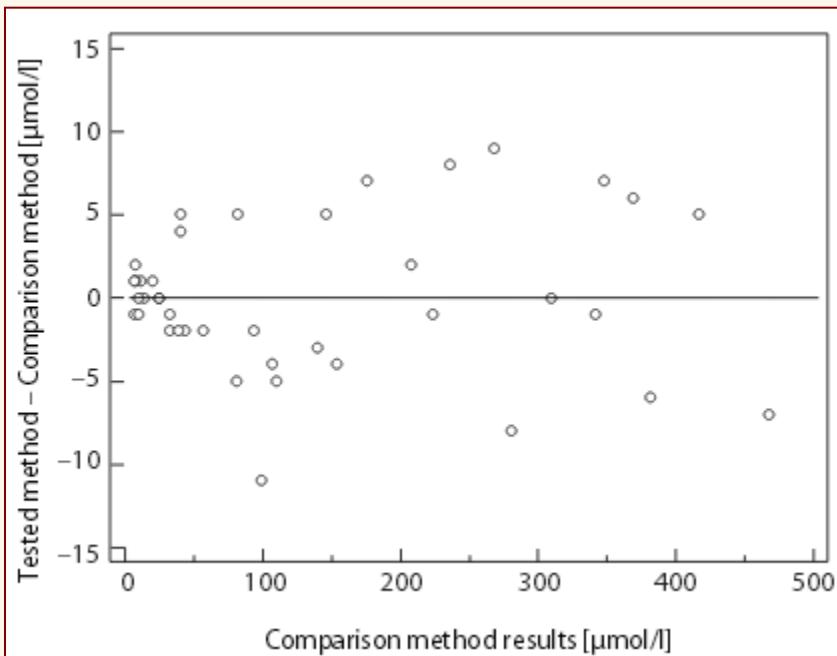
Method X	HBbefM1				
Method Y	HBbefM2				
Method	Mean	Coefficient of variation (%)			
X	142,4138	3,00			
Y	142,6207	3,00			
Sample size			29		
Variance ratio			0,9971		
<b>Regression Equation</b>					
$y = -11,4848 + 1,0821 \times$					
Parameter	Coefficient	Std. Error	95% CI		
Intercept	-11,4848	6,4452	-24,6872 to 1,7176		
Slope	1,0821	0,04595	0,9880 to 1,1762		



# Bland-Altmanov grafikon



# Bland-Altmanov grafikon



# Bland-Altmanov grafikon

Lessons in biostatistics

*Biochemia Medica* 2015;25(2):141–51

## Understanding Bland Altman analysis

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The Statistician 32 (1983) 307-317  
© 1983 Institute of Statisticians

## Measurement in Medicine: the Analysis of Method Comparison Studies†

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‡ Department of Clinical Epidemiology and Biostatistics, St George's Hospital Medical School, Cranmer Terrace, London SW17 0RE, UK

**Summary:** Methods of analysis used in measurement comparison studies are reviewed. The use of correlation coefficients to assess agreement between means is criticized. A simple procedure for the analysis of variance and simple graphical methods are described.

*Lancet*, 1986 Feb 8;1(8476):307-10.

## Statistical methods for assessing agreement between two methods of clinical measurement.

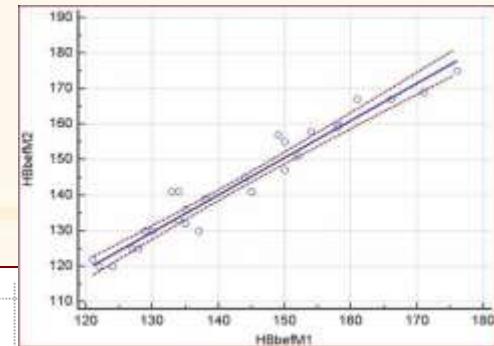
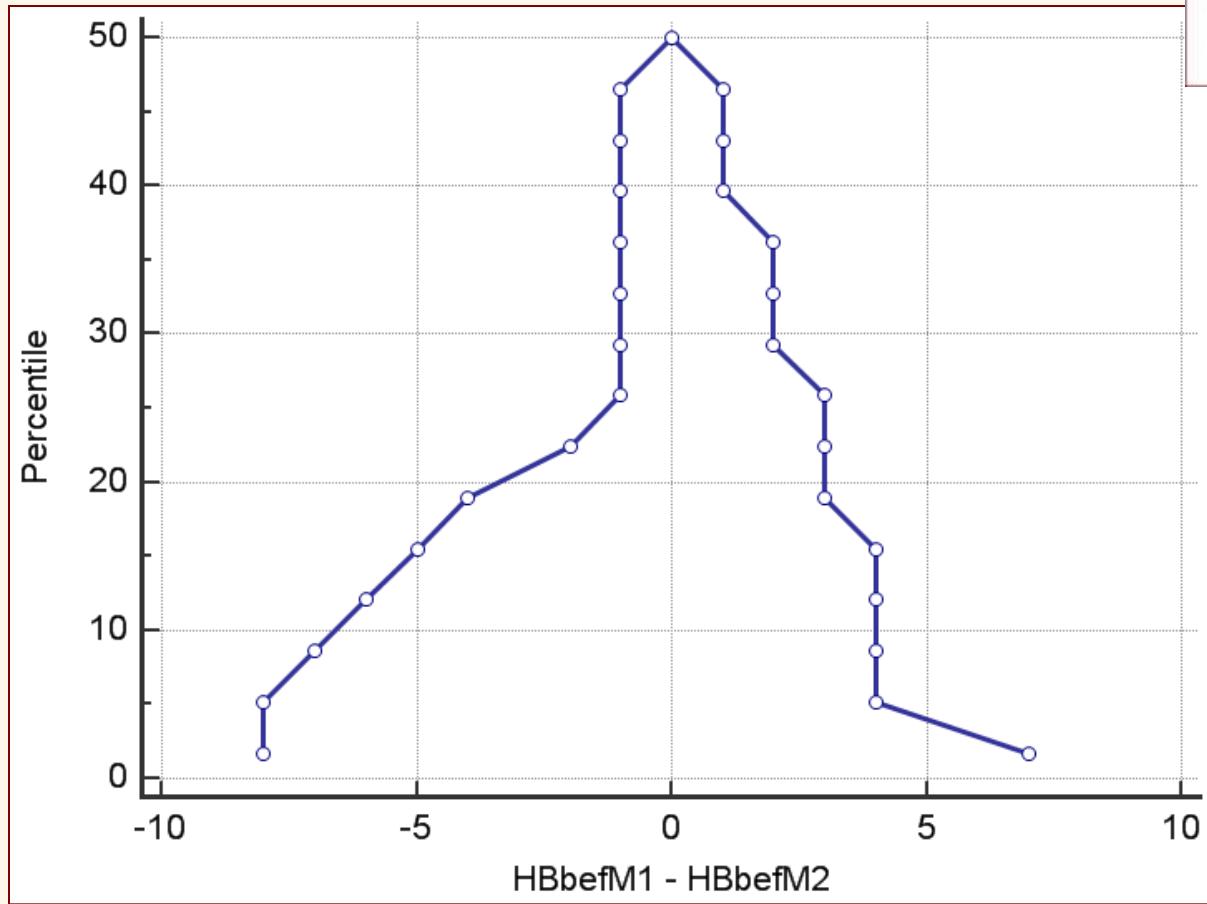
Bland JM, Altman DG.

### Abstract

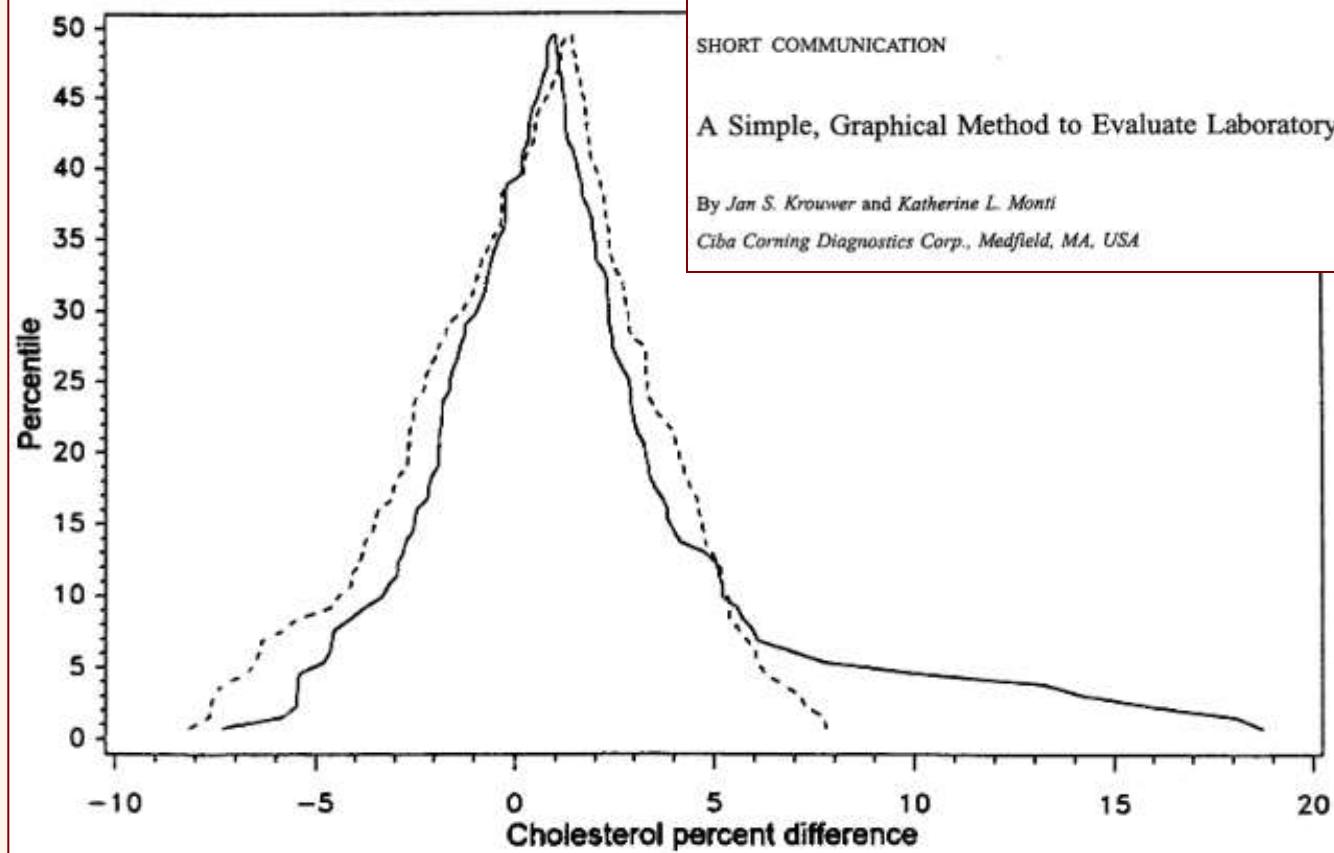
In clinical measurement comparison of a new measurement technique with an established one is often needed to see whether they agree sufficiently for the new to replace the old. Such investigations are often analysed inappropriately, notably by using correlation coefficients. The use of correlation is misleading. An alternative approach, based on graphical techniques and simple calculations, is described, together with the relation between this analysis and the assessment of repeatability.



# Krouwer-Montijev grafikon



# Krouwer-Montijev grafikon



# Mjere podudarnosti/slaganja

Table 3. Contingency table for measuring interrater reliability using measures of agreement (data present arbitrary distribution of N = 38 samples of negative, positive and highly positive findings of immunofluorescent patterns of antineutrophil cytoplasmic antibodies (ANCA) by two independent observers)\*

Observers		Observer B			Total (N)
		negative (N)	positive (N)	highly positive (N)	
Observer A	negative (N)	9	1	0	10
	positive (N)	2	12	3	17
	highly positive (N)	1	0	10	1
Total (N)		12	13	13	38
Measures of agreement		$\kappa$	0.72		
		$\kappa_{LW}$	0.75		
		$\kappa_{QW}$	0.78		
		W	0.78		
		ICC	0.78		

\*Abbreviations: N – number of subjects,  $\kappa$  – kappa statistics, LW – linear weight, QW – quadratic weight, W – concordance coefficient, ICC – interclass correlation coefficient.



# Zaključak

- Usporedba mjernih postupaka
  - ✓ Bland-Altmanov grafikon
  - ✓ Krouwer-Montijev grafikon
  - ✓ Passing-Bablokova regresija
  - ✓ Demingova regresija
  - ✓ koeficijent konkordancije W
  - ✓ interklasni koeficijent korelacije (ICC)
  - ✓ Cohenov  $\kappa$



# Hvala na pozornosti



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